

Table 2
Coordinate System Conversion Formulas

Coordinate System	Scalar Conversions	Vector Conversions
Cylindrical (r, ϕ, z)	$x = r \cos \phi$ $y = r \sin \phi$ $z = z$ $r = \sqrt{x^2 + y^2}$ $\phi = \tan^{-1}(y/x)$ $z = z$	$u_x = \cos \phi u_r - \sin \phi u_\phi$ $u_y = \sin \phi u_r + \cos \phi u_\phi$ $u_z = u_z$ $u_r = \cos \phi u_x + \sin \phi u_y$ $u_\phi = -\sin \phi u_x + \cos \phi u_y$ $u_z = u_z$
Spherical (R, θ, ϕ) ($0 \leq \theta \leq \pi$)	$x = R \sin \theta \cos \phi$ $y = R \sin \theta \sin \phi$ $z = R \cos \theta$ $R = \sqrt{x^2 + y^2 + z^2}$ $\phi = \tan^{-1} \left(\frac{\sqrt{x^2 + y^2}}{z} \right)$ $\phi = \tan^{-1}(y/x)$	$u_x = \sin \theta \cos \phi u_R + \cos \theta \cos \phi u_\theta - \sin \phi u_\phi$ $u_y = \sin \theta \sin \phi u_R + \cos \theta \sin \phi u_\theta + \cos \phi u_\phi$ $u_z = \cos \theta u_R - \sin \theta u_\theta$ $u_R = \sin \theta \cos \phi u_x + \sin \theta \sin \phi u_y + \cos \theta u_z$ $u_\theta = \cos \theta \cos \phi u_x + \cos \theta \sin \phi u_y - \sin \theta u_z$ $u_\phi = -\sin \phi u_x + \cos \phi u_y$